

# PROBABILISTIC RESOURCE ANALYSIS

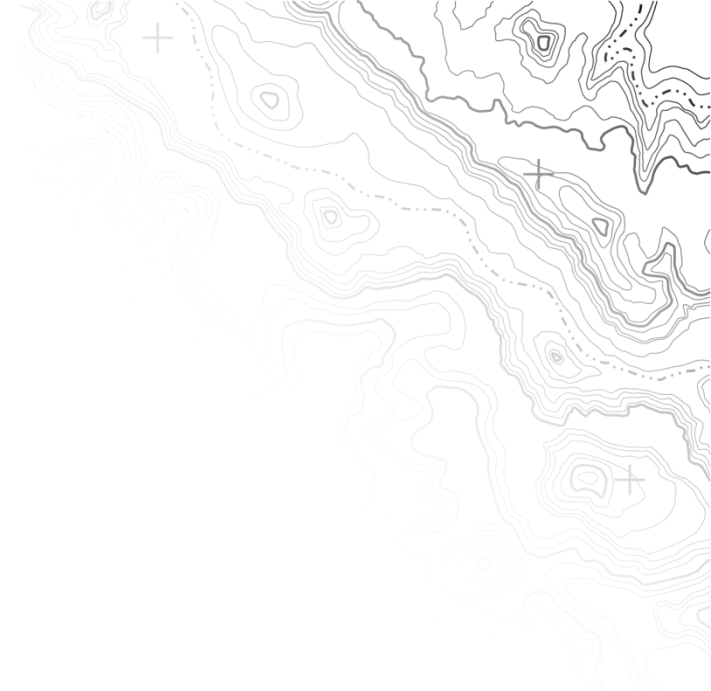
presented by Letha Lencioni  
Society of Petroleum Evaluation Engineers 56<sup>th</sup> Annual Conference  
Lake Louise, Alberta, Canada  
June 11, 2019

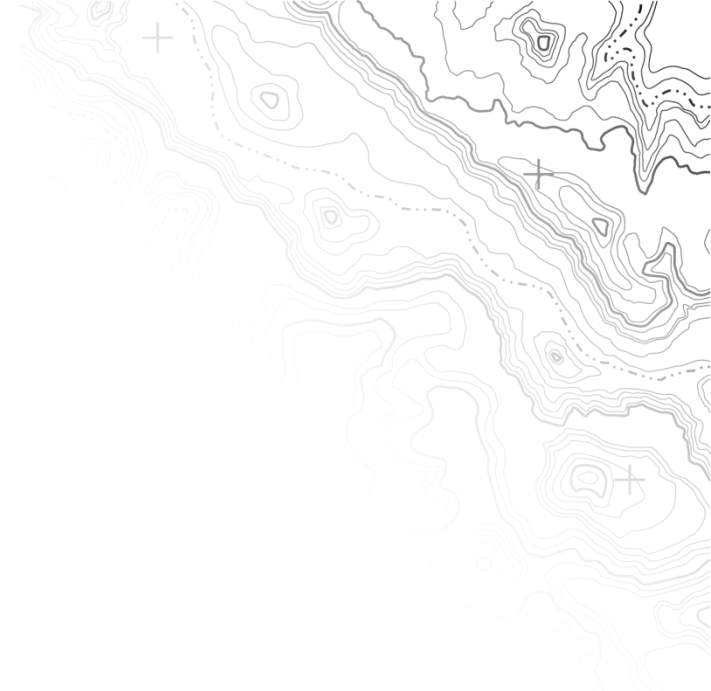


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# Outline

- What are resources?
  - Definitions
  - Reasons for estimating
- Probabilistic analysis
  - Basic concepts
  - History in industry
  - Software
- Estimation of resources
  - Input data and distributions
  - Running the software
  - Evaluating results
- Examples





# WHAT ARE RESOURCES?

# What are resources?

- PRMS

“Petroleum resources are the quantities of hydrocarbons naturally occurring on or within the Earth’s crust.”

The term “resources” encompasses all petroleum quantities, including discovered and undiscovered (recoverable and unrecoverable) plus quantities already produced, or Petroleum Initially in Place (PIIP).

- COGEH – same definitions

# Classification of Resources

- Resources are classified into
  - Discovered
    - Reserves
    - Contingent Resources
    - Unrecoverable
  - Undiscovered
    - Prospective Resources
    - Unrecoverable

# Classification of Resources

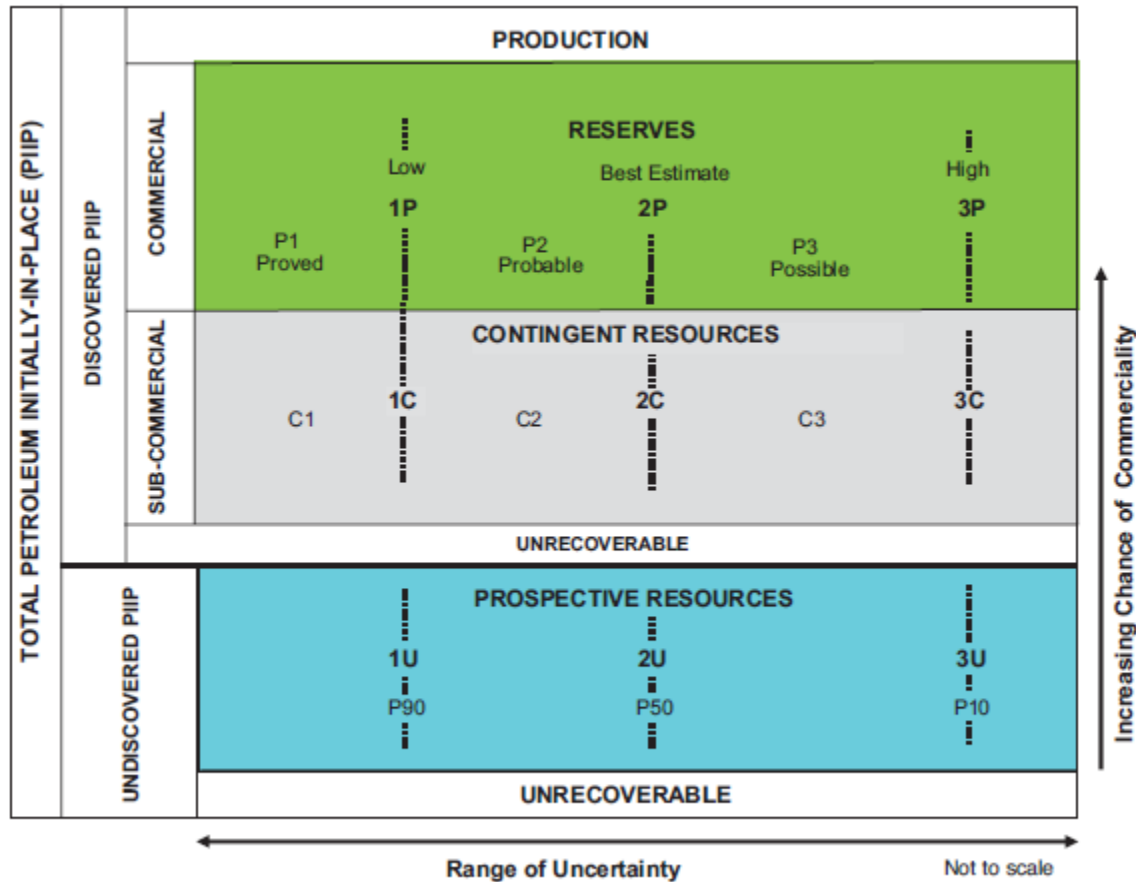


Figure 1.1—Resources classification framework

# Definitions

- Reserves
  - “those quantities of petroleum anticipated to be commercially recoverable by application of development projects to known accumulations from a given date forward under defined conditions.”
- Contingent Resources
  - “those quantities of petroleum estimated, as of a given date, to be potentially recoverable from known accumulations, by the application of development project(s) not currently considered to be commercial owing to one or more contingencies.”

# Definitions

- Prospective Resources
  - “those quantities of petroleum estimated, as of a given date, to be potentially recoverable from undiscovered accumulations by application of future development projects.”
- This presentation focuses on Contingent and Prospective Resources

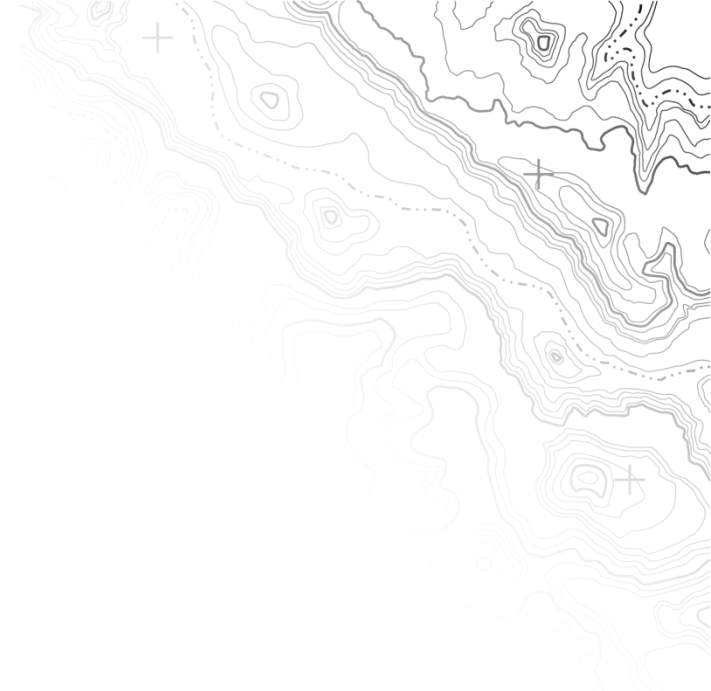


# Reasons for Estimating

- Evaluation of exploration targets
  - Ranking of prospects
  - Make development plans that can cover the range of possible outcomes
  - Provide a range of production forecasts to evaluate the expected outcome of their ventures
  - Measure exploration, appraisal, and commercial risks
  - Ensure that they can handle an unfavorable outcome (i.e., that they have an economic project, even if the low case materializes)
  - Understand and communicate the confidence level of their reserves estimate
  - Appraisal of market value of undeveloped acreage
    - Could be considered too hypothetical
    - May be appropriate for some times and places, i.e. Alaska in mid-70s

# Reasons for Estimating

- Regulatory reporting
  - The following exchanges allow reporting of Contingent and Prospective Resources
    - Canada (TSX Venture)
    - Australia (ASX)
    - London (AIM)
    - Hong Kong (HKEx)

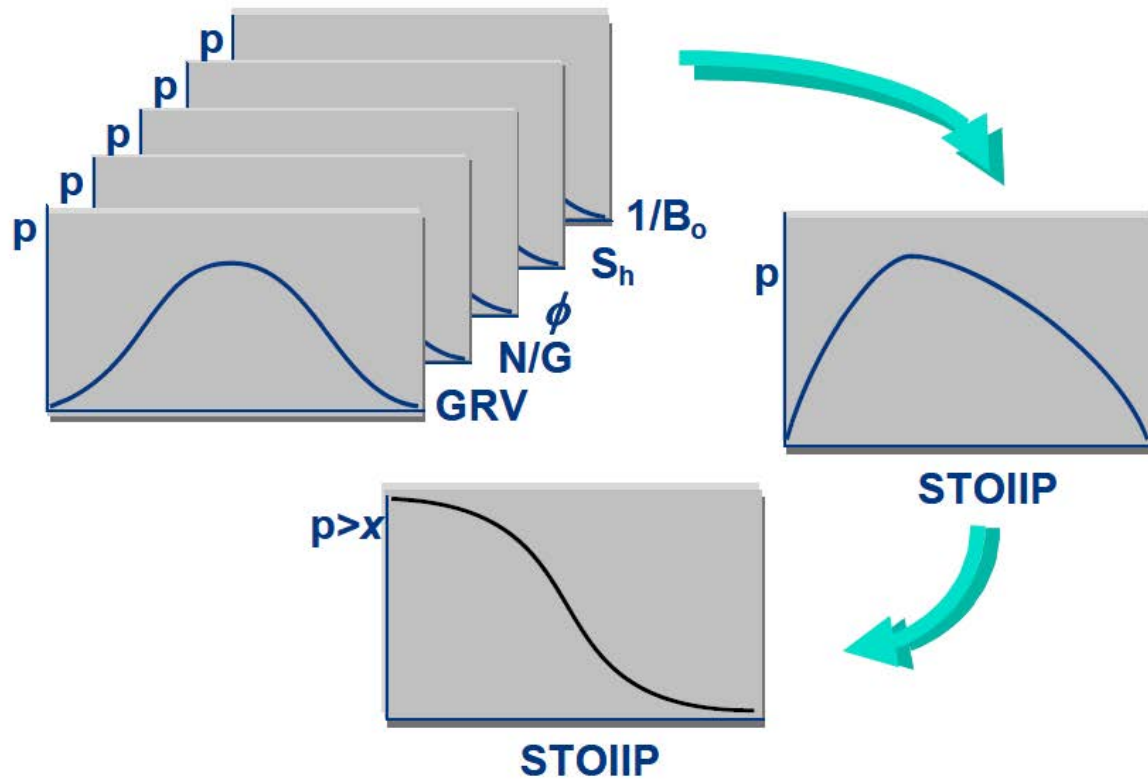


# PROBABILISTIC ANALYSIS

# Basic Concepts

- PRMS Definition:  
“The method of estimation of resources is called probabilistic when the known geoscience, engineering, and economic data are used to generate a continuous range of estimates and their associated probabilities.”
- May also be called stochastic, or Monte Carlo analysis
- User defines the uncertainty distributions of the input parameters (input distributions) and the relationship (correlations) between them
- Method involves repeated random sampling of input distributions to generate a resulting distribution (such as recoverable petroleum quantities)

# Probabilistic Approach to Volumetrics



From PRMS Guidelines, Nov. 2011

# History in Petroleum Industry

- Probabilistic analysis has long been used in the industry

## Technical papers

- From 1961 discusses “operations research” and stochastic analysis
- From 1962 mentions Monte Carlo analysis applied to decision making
- From 1965 on fundamentals and applications of Monte Carlo method

## Books

- Newendorp, 1975
- Megill, 1977?

1984 WPC classification system including probabilistic definitions.

First included in SPE definitions in 1997.

# Software for Monte Carlo Analysis

- Most common in the industry
  - @Risk by Palisade
  - Crystal Ball by Oracle
- Others
  - Quantum XL by SigmaZone
  - DiscoverSim by Sigma XL
  - Premium Solver V7.0 + Risk Solver V7.0 by Frontline Systems
  - GoldSim by GoldSim
  - Analytica by Lumina
  - Excel
- Most are add-ins to Excel except Analytica

# Estimation of Resources

- Volumetric
  - Seismic-based prospects
  - Gravity / aero-mag leads
  - Surface expressions
- Analog performance based
- Statistical/Other



# Input Data and Distributions

## Volumetric analysis of identified prospect

- Area } OR • Bulk reservoir volume
- Net pay }
- Porosity
- Water / hydrocarbon saturation
- Formation volume factors
- Recovery factor
- Ratios of secondary product

# Data Considerations

- Type of distribution
  - Triangular
    - most commonly used when little data available
    - minimum, most likely, maximum or
    - P90, most likely, P10
  - can greatly over/underestimate parameter if distribution is highly skewed
- Others
  - fit a larger group of data
  - select better representation of skewed data

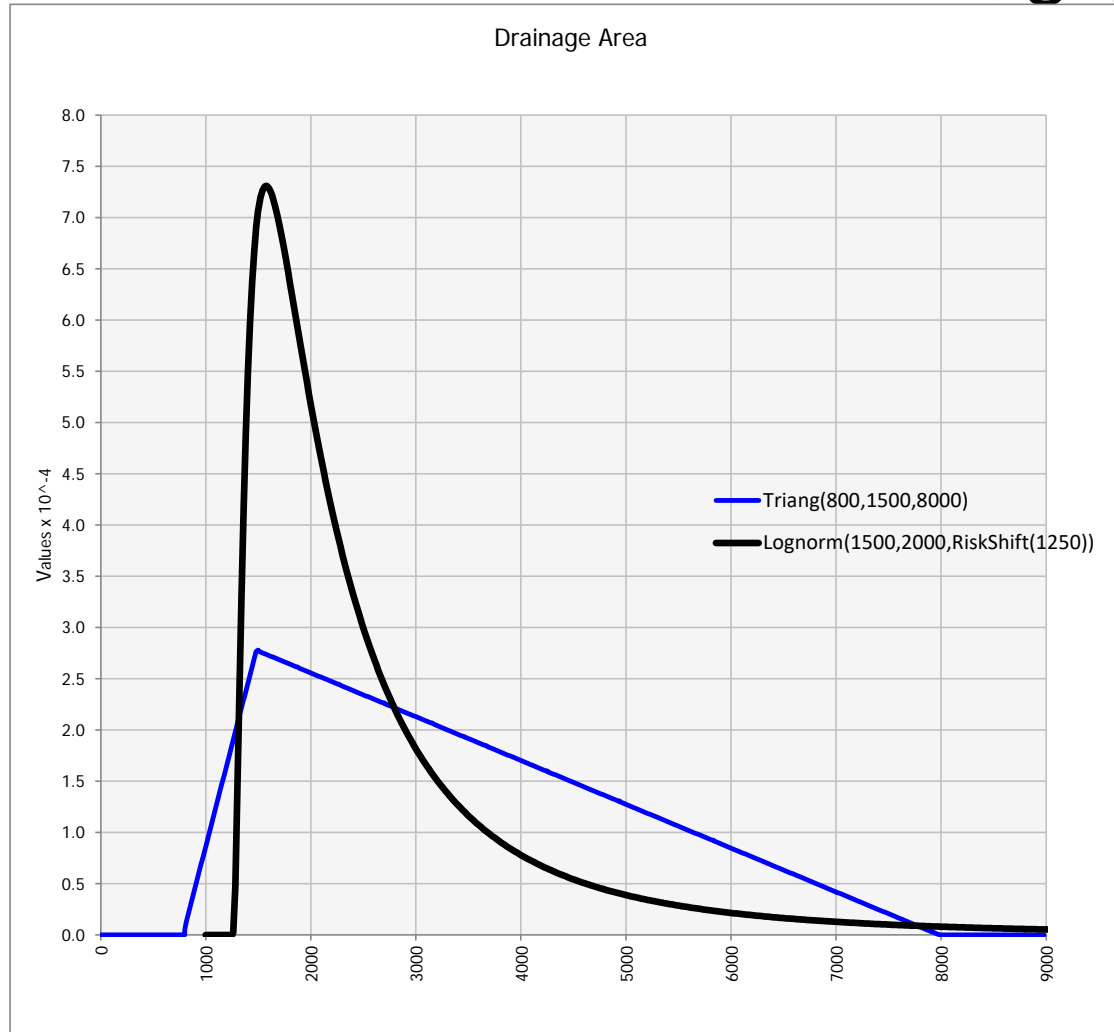
# Data Considerations

- Risk of failure is incorporated in another way
  - Separate POS applied for economic analysis
  - Do not include porosity, area, or hydrocarbon saturation of zero
  - We are calculating prospective resources if a successful discovery is made
- Remember, input range represents range of average reservoir properties, not range seen in any well or any specific point in reservoir

# Data Considerations

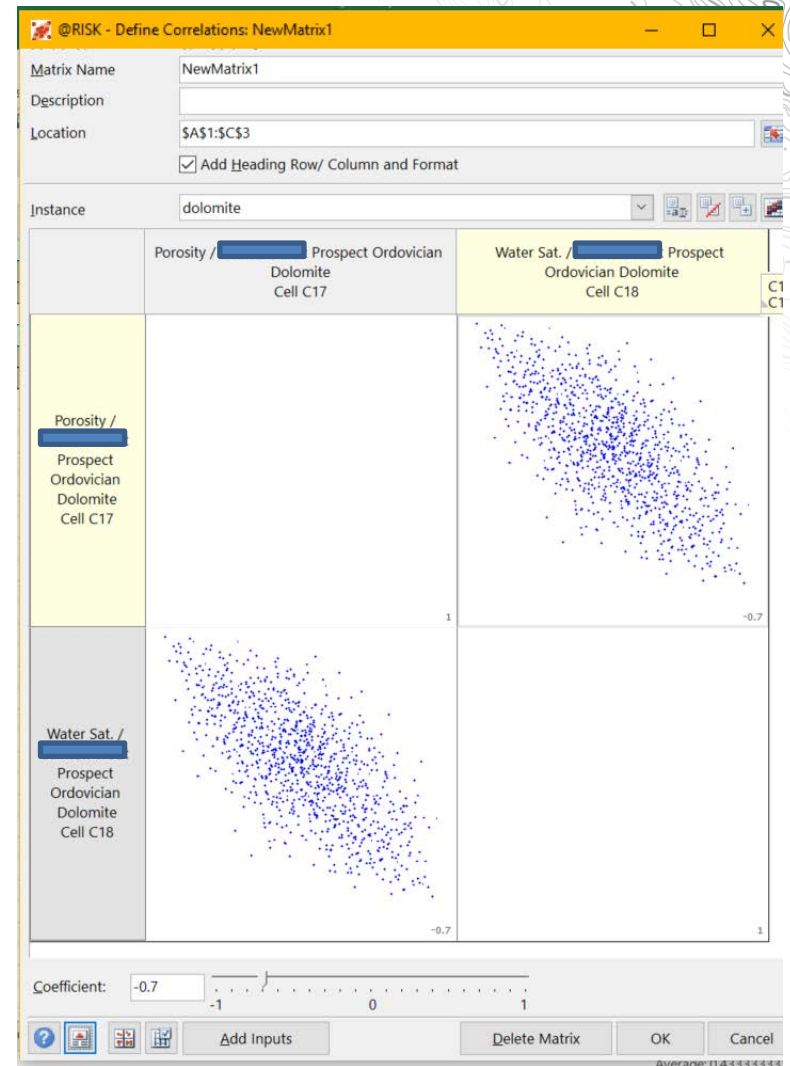
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- Remember, input range represents range of average reservoir properties, not range seen in any well or any specific point in reservoir

# Comparison of Triangular and Lognormal Distributions with Similar Ranges



# Correlation of Input Parameters

- Positive Correlation
  - Net pay and productive area
- Negative Correlation
  - Porosity and water saturation

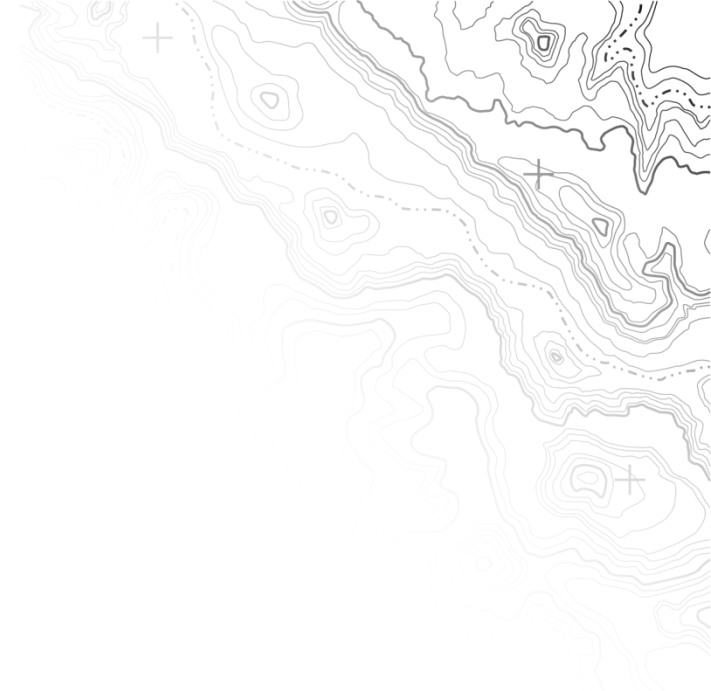


# Running the Program

- 5,000 iterations usually sufficient for simple models
- Large, complex models may require 40,000

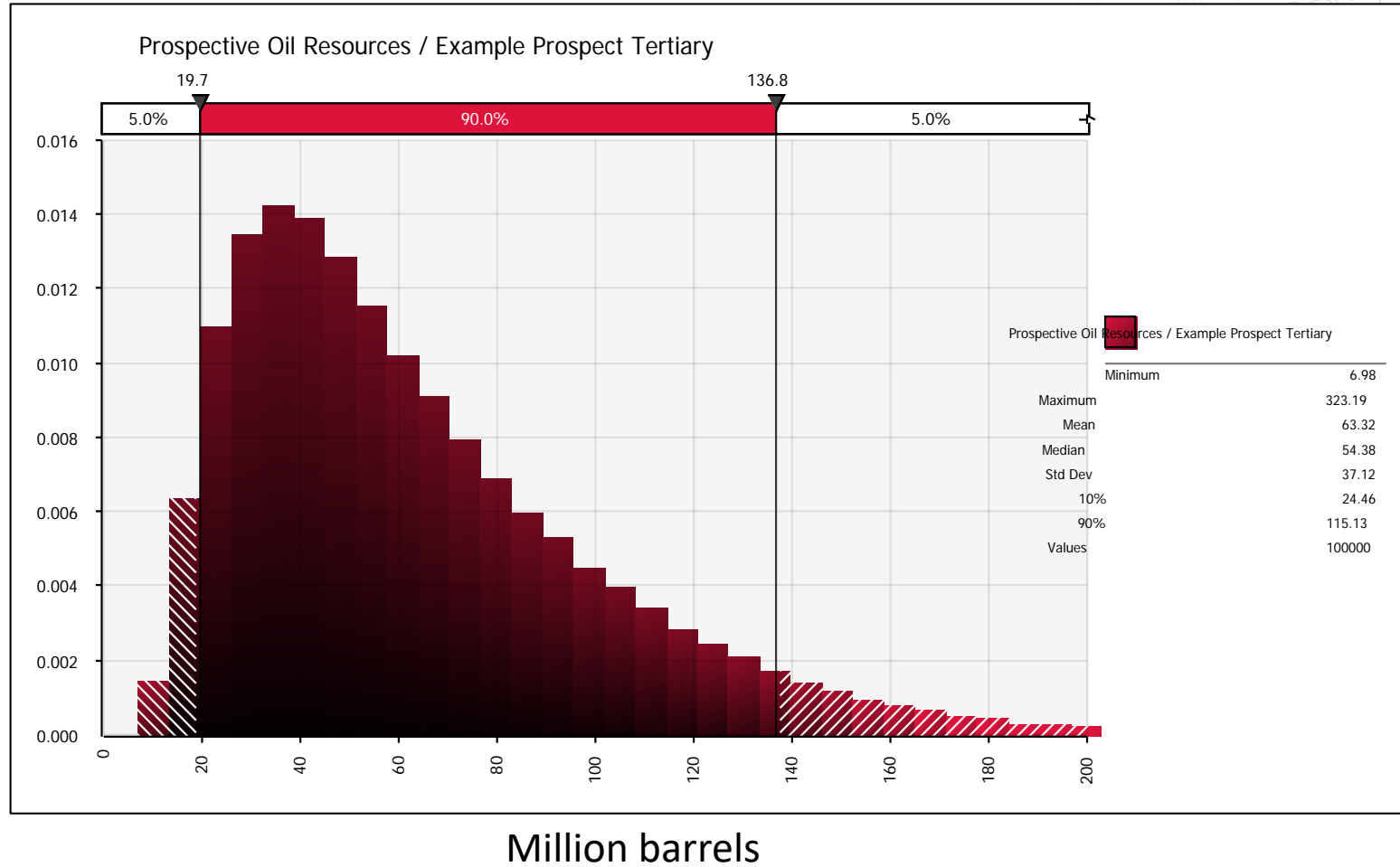
# Output

- Built-in graphical output
  - Output distributions
  - Tornado plots
  - Summary trend plots
- Excel output of inputs and results
- Plots made with Excel output

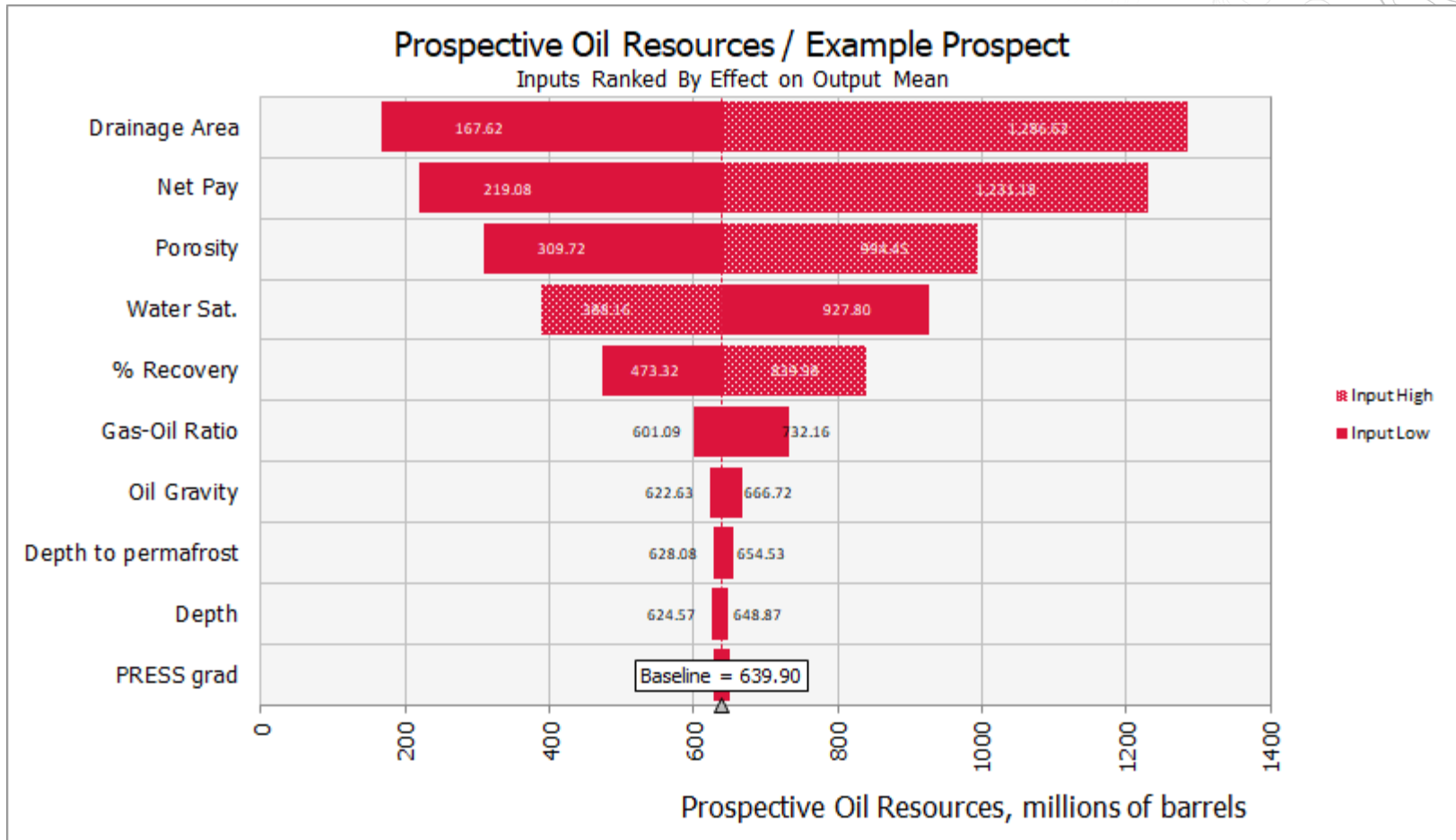




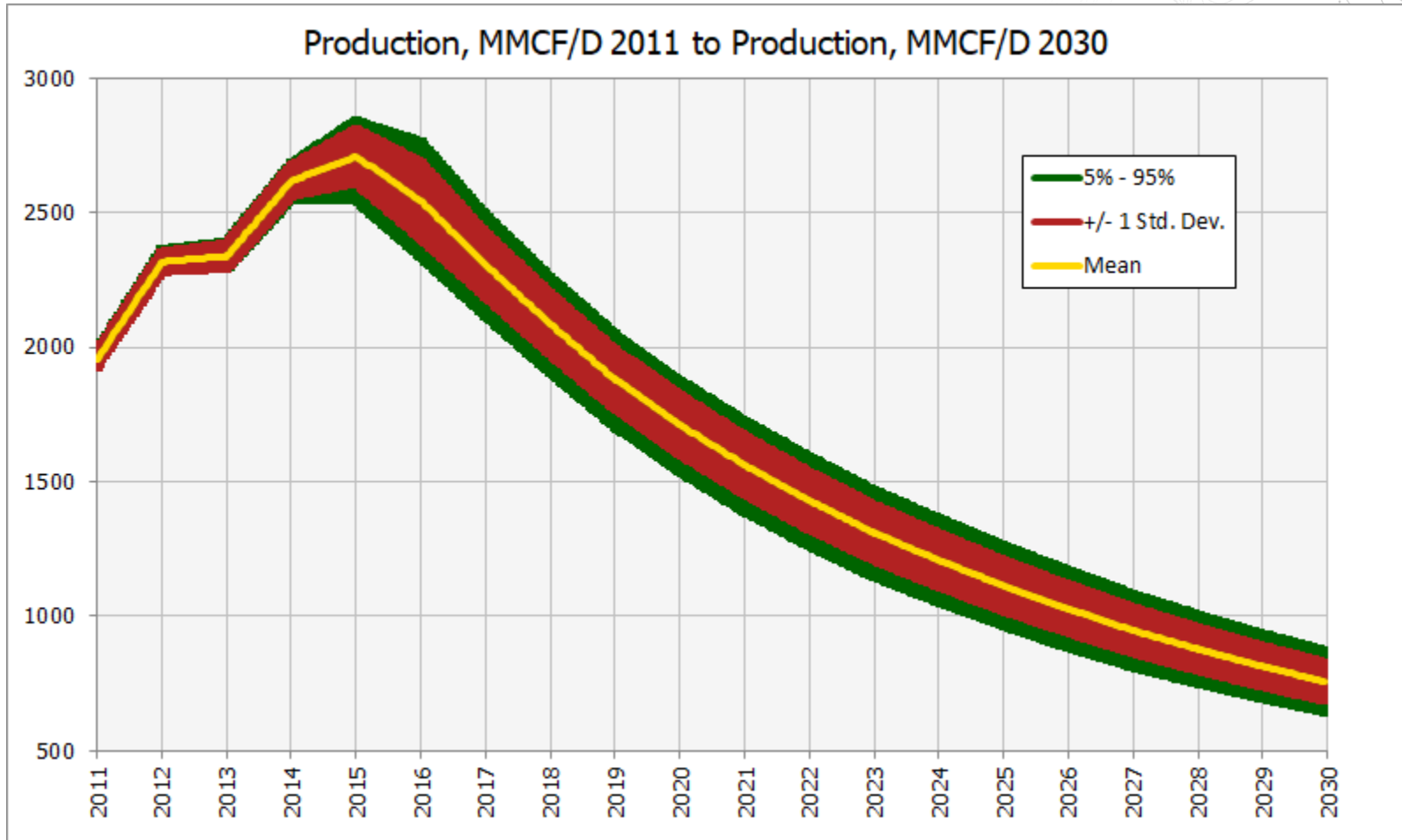
# Output Distributions



# Tornado Plot



# Summary Trend Plot



# Output to Excel

## @RISK Detailed Statistics

Performed By: Chen, Ting T.

Date: Friday, September 7, 2018 11:45:37 AM

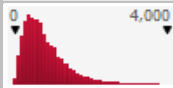
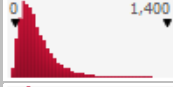
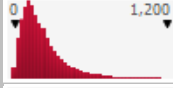
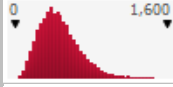
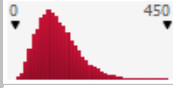
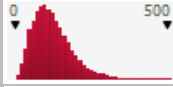

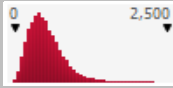
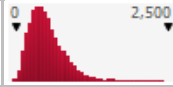
Name	Prospective Resources - Oil in Place / KB (Tert)	Prospective Oil Resources / KB (Tert)	Prospective Assoc. Gas Resources / KB (Tert)	Prospective Resources - Oil in Place / DJ (U Cret)	Prospective Oil Resources / DJ (U Cret)	Prospective Assoc. Gas Resources / DJ (U Cret)	Prospective Resources - Oil in Place / KG	Prospective Oil Resources / KG	Prospective Assoc. Gas Resources / KG	Prospective Resources - Oil in Place / KD (U Cret)
Description	Output	Output	Output	Output	Output	Output	Output	Output	Output	Output
Cell	KB (Tert)!C22	KB (Tert)!C23	KB (Tert)!C24	DJ (U Cret)!C22	DJ (U Cret)!C23	DJ (U Cret)!C24	KG!C22	KG!C23	KG!C24	KD (U Cret)!C22
Minimum	119.2	29.3	30.4	105.4	23.6	24.9	348.6	84.4	65.8	364.7
Maximum	3,721.1	1,229.3	1118.7	1,430.7	441.9	498.6	7,102.8	2,227.9	2358.1	8,244.8
Mean	877.2	239.6	237.0	499.7	136.5	134.9	2,113.5	577.8	571.0	2,319.0
Std Deviation	475.6	133.6	137.5	187.0	53.8	56.8	847.4	243.3	254.6	1,097.8
Variance	226197.6	17838.99	18901.14	34971.57	2891.9	3231.673	718130.9	59194.8	64810.54	1205264
Skewness	1.248811	1.327508	1.348992	0.672334	0.7685375	0.8933885	0.7447173	0.8522304	0.950909	1.033043
Kurtosis	5.062639	5.477387	5.304563	3.469089	3.710736	4.085405	3.65677	4.050351	4.398961	4.406108
Errors	0	0	0	0	0	0	0	0	0	0
Mode	596.7	138.0	149.5	420.4	116.9	107.2	1,811.2	547.2	429.9	1,757.5
5% Perc	304.7	81.0	77.0	233.2	62.0	58.2	929.9	245.3	230.6	899.1
10% Perc	373.4	100.2	94.8	276.2	73.0	69.3	1,108.9	295.0	277.6	1,101.3
15% Perc	431.9	115.7	110.6	307.3	82.0	77.9	1,247.8	331.9	317.1	1,256.2
20% Perc	480.1	129.4	124.8	335.7	90.0	86.1	1,369.1	366.7	354.5	1,383.6
25% Perc	524.9	141.8	138.1	362.4	96.8	93.1	1,489.5	398.9	386.2	1,516.9
30% Perc	573.2	154.7	150.5	387.0	103.4	99.8	1,594.7	429.1	415.3	1,626.6
35% Perc	620.3	167.8	163.1	409.6	110.1	106.7	1,700.2	458.0	444.2	1,747.9
40% Perc	670.1	181.5	176.0	431.3	116.4	113.0	1,802.4	486.0	473.4	1,866.8
45% Perc	719.8	195.1	189.2	453.9	122.7	119.4	1,899.4	513.2	500.8	1,979.9
50% Perc	772.5	209.3	204.0	478.7	129.1	126.2	2,008.4	545.0	532.3	2,113.2
55% Perc	825.2	224.3	220.2	501.3	136.1	133.5	2,112.0	573.6	564.9	2,253.0
60% Perc	891.1	240.7	237.5	526.3	143.2	140.8	2,215.2	604.7	593.6	2,401.2
65% Perc	959.2	261.0	256.0	552.7	150.9	148.5	2,337.4	638.8	629.1	2,551.2
70% Perc	1,038.0	282.7	276.7	580.8	159.0	157.7	2,469.3	678.7	669.7	2,722.2
75% Perc	1,124.1	306.5	301.5	612.6	168.4	167.3	2,619.6	720.3	713.6	2,925.4
80% Perc	1,221.9	334.4	332.9	650.2	179.1	178.6	2,795.6	767.1	764.4	3,150.6
85% Perc	1,348.0	369.7	370.2	695.0	192.0	192.6	3,003.8	825.1	833.0	3,449.3
90% Perc	1,520.8	419.0	424.9	752.5	209.7	211.2	3,259.7	904.9	913.6	3,812.2
95% Perc	1,799.7	502.2	511.5	842.5	237.0	241.5	3,666.4	1,030.3	1042.5	4,389.6

# Output to Excel

## @RISK Output Results

Performed By: Chen, Ting T.

Date: Friday, September 7, 2018 11:45:33 AM

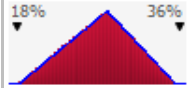
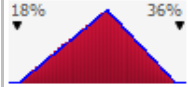
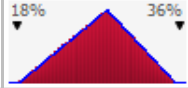
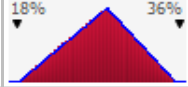
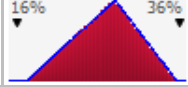
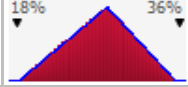
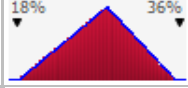
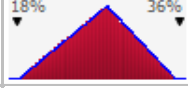
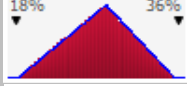
Name	Worksheet	Cell	Graph	Min	Mean	Max	5%	95%	Errors
Prospective Resources - Oil in Place / KB (Tert)	KB (Tert)	C22		119.2	877.2	3,721.1	304.7	1,799.7	0
Prospective Oil Resources / KB (Tert)	KB (Tert)	C23		29.3	239.6	1,229.3	81.0	502.2	0
Prospective Assoc. Gas Resources / KB (Tert)	KB (Tert)	C24		30.4	237.0	1,118.7	77.0	511.5	0
Prospective Resources - Oil in Place / DJ (U Cret)	DJ (U Cret)	C22		105.4	499.7	1,430.7	233.2	842.5	0
Prospective Oil Resources / DJ (U Cret)	DJ (U Cret)	C23		23.6	136.5	441.9	62.0	237.0	0
Prospective Assoc. Gas Resources / DJ (U Cret)	DJ (U Cret)	C24		24.9	134.9	498.6	58.2	241.5	0
Prospective Resources - Oil in Place / KG	KG	C22		348.6	2,113.5	7,102.8	929.9	3,666.4	0
Prospective Oil Resources / KG	KG	C23		84.4	577.8	2,227.9	245.3	1,030.3	0
Prospective Assoc. Gas Resources / KG	KG	C24		65.8	571.0	2,358.1	230.6	1,042.5	0

# Output to Excel

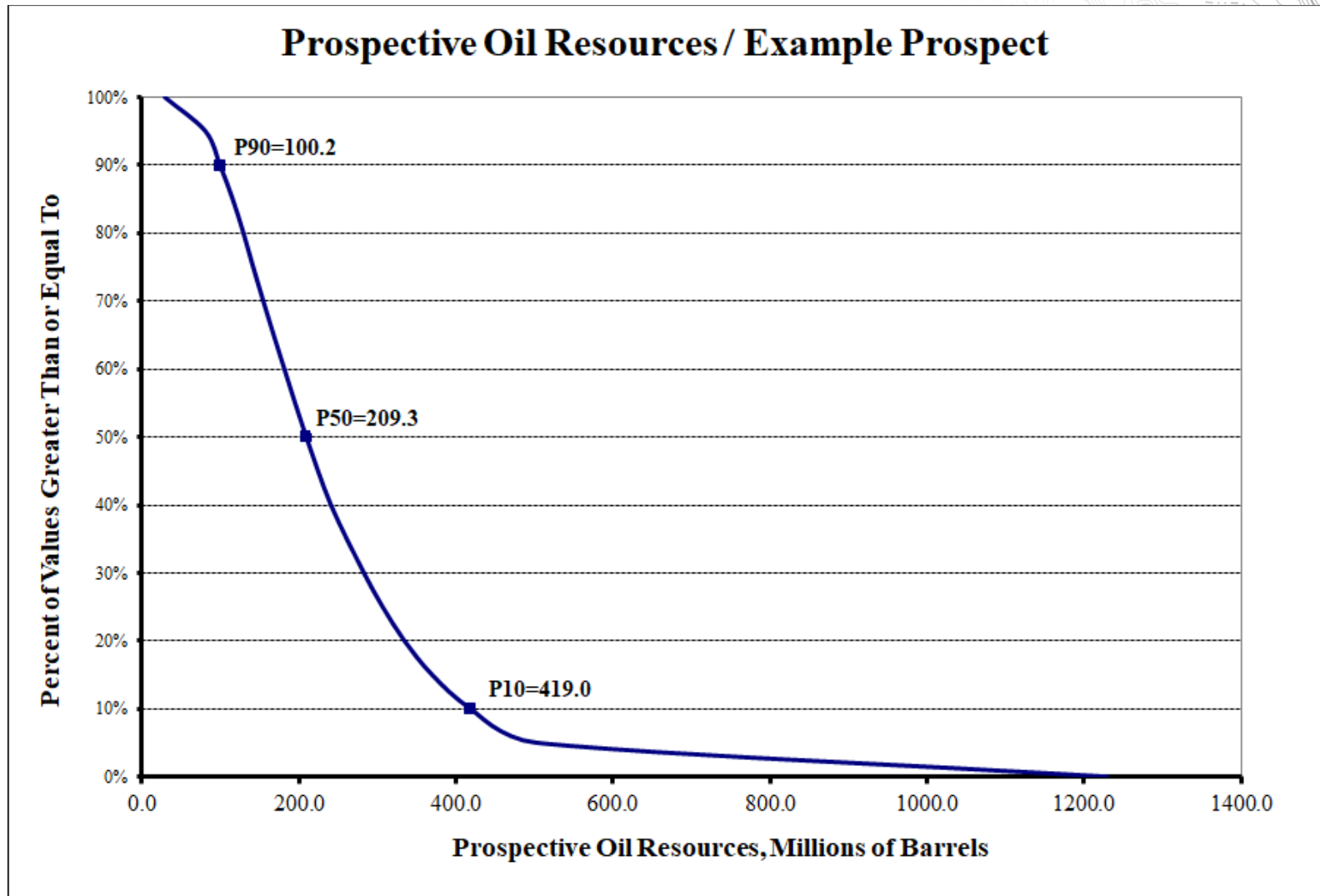
## @RISK Input Results

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Date: Friday, September 7, 2018 11:45:19 AM

Name	Worksheet	Cell	Graph	Min	Mean	Max	5%	95%	Errors
Category: % Recovery									
% Recovery / KB (Tert)	KB (Tert)	C20		19.0%	27.3%	34.9%	21.7%	32.6%	0
% Recovery / DJ (U Cret)	DJ (U Cret)	C20		19.1%	27.3%	34.9%	21.7%	32.6%	0
% Recovery / KG	KG	C20		19.0%	27.3%	34.9%	21.7%	32.6%	0
% Recovery / KD (U Cret)	KD (U Cret)	C20		19.1%	27.3%	34.9%	21.7%	32.6%	0
% Recovery / latuk-D (U Cret)	latuk-D (U Cret)	C20		18.1%	27.0%	35.0%	20.9%	32.6%	0
% Recovery / KC (U Cret)	KC (U Cret)	C20		19.1%	27.3%	34.9%	21.7%	32.6%	0
% Recovery / Amatuk (U Cret)	Amatuk (U Cret)	C20		19.1%	27.3%	35.0%	21.7%	32.6%	0
% Recovery / MJ-3 (U Cret)	MJ-3 (U Cret)	C20		19.1%	27.3%	34.9%	21.7%	32.6%	0
% Recovery / MJ-4 (U Cret)	MJ-4 (U Cret)	C20		19.1%	27.3%	34.9%	21.7%	32.6%	0

# Output Distributions from Excel



# Aggregation

- If we sum of  $P_{90}$  values for several prospects, we assume full dependence -- that all prospects will experience their low case simultaneously
- This results in a value with greater certainty than  $P_{90}$
- Addition of  $P_{10}$  values results in a value with lower probability than 10%
- Statistical aggregation can avoid this
- Sometimes dependencies should be incorporated, which can be accounted for in the Monte Carlo software



# Aggregation

- 2018 PRMS recommends:
  - For reporting purposes, assessment results should not incorporate statistical aggregation beyond the field, property, or project level.
  - Results reported beyond this level should use arithmetic summation by category but should caution that the aggregate  $P_{90}$  may be a very conservative estimate and aggregate  $P_{10}$  may be very optimistic, depending on the number of items in the aggregate.
- COGEH (2005)
  - When a probabilistic approach is used, Reported Reserves are derived by arithmetic summation of discrete property reserves estimates for each reserves category resulting from separate probabilistic analyses.

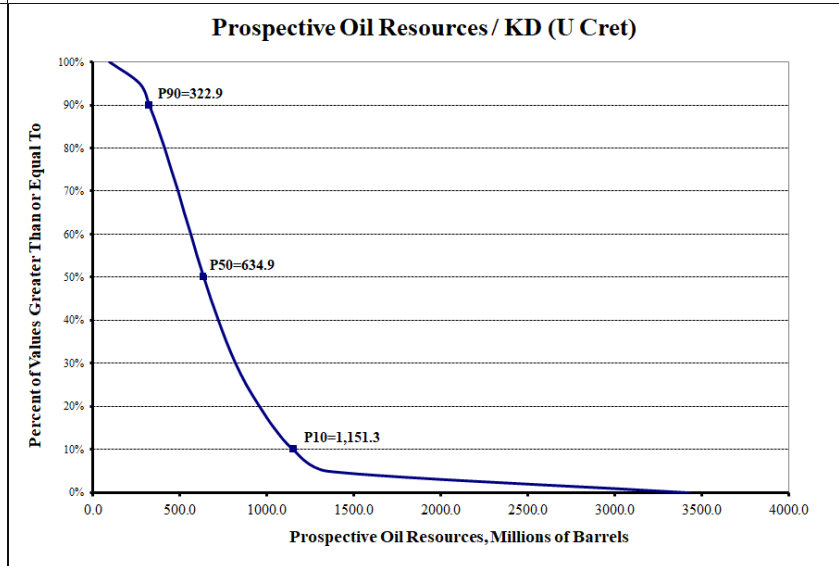
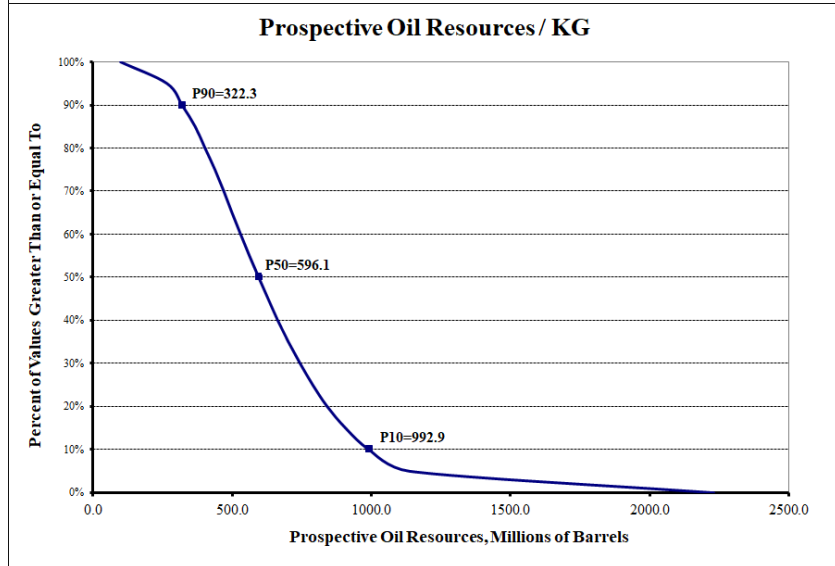
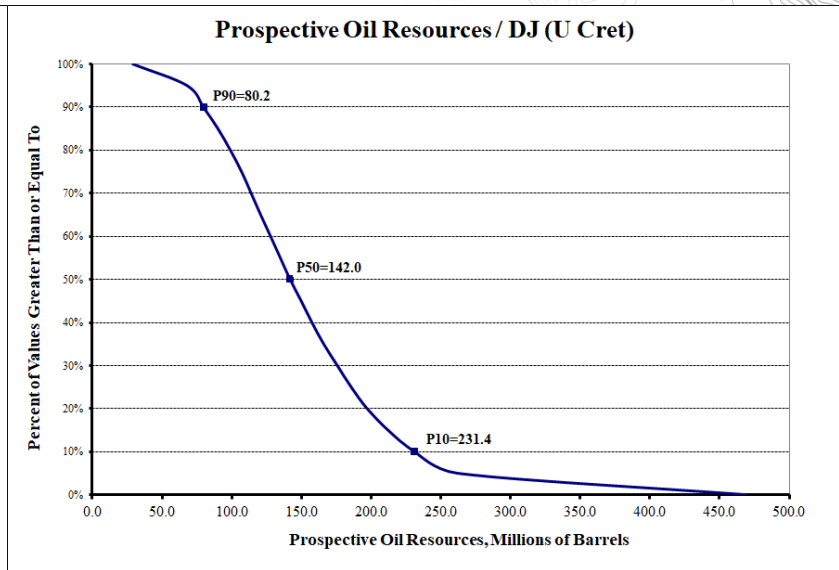
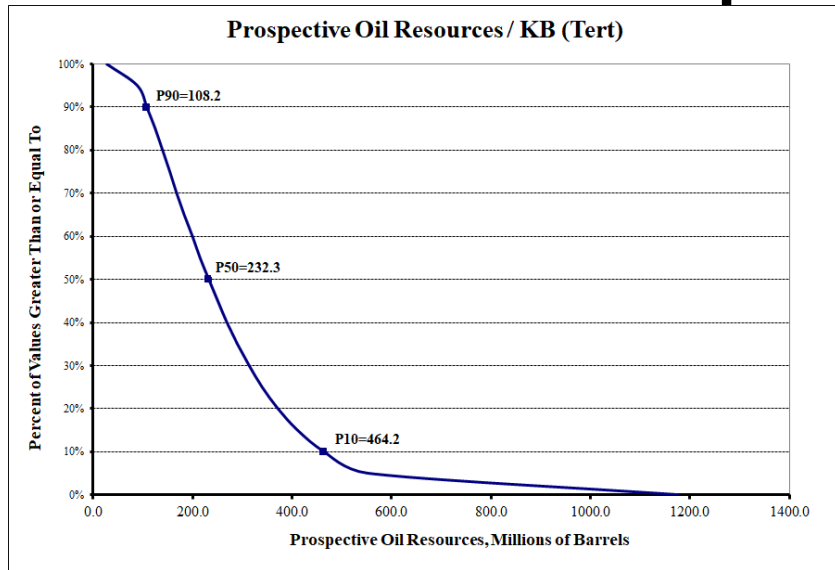
# Offshore Guyana Example

- Conventional prospects delineated by seismic
- Numerous prospects, varying target horizons
- Volumetrics calculated probabilistically to estimate Prospective Resources

# Input Data (partial)

LEAD	KB (Tert)			DJ (U Cret)			KG (U Cret)		
	Minimum	Most Likely	Maximum	Minimum	Most Likely	Maximum	Minimum	Most Likely	Maximum
Oil Gravity	30	35	40	30	35	40	30	35	40
Gas-Oil Ratio	100	500	1,000	500	1,000	1,500	500	1,000	1,500
Gas Gravity	0.65	0.70	0.75	0.65	0.70	0.75	0.65	0.70	0.75
Pgr, psi	0.44	0.45	0.48	0.44	0.45	0.48	0.44	0.45	0.48
Depth, m	3,660	3,700	3,740	4,060	4,160	4,230	3,400	3,900	4,050
Porosity	15	25	30	15	22	30	15	22	30
Water Sat.	20	30	40	20	30	40	20	30	40
Drainage area, km <sup>2</sup>	17	27	43	14	24	30	17	30	34
Gross Thickness, m	60	70	125	40	50	60	200	275	325
Net/Gross, fraction	0.45	0.55	0.75	0.50	0.70	0.80	0.25	0.45	0.65
% Recovery	19.00	28.00	35.00	19.00	28.00	35.00	19.00	28.00	35.00
LEAD	Kumaka (U Cret)			Iatuk-D (U Cret)			KC (U Cret)		
	Minimum	Most Likely	Maximum	Minimum	Most Likely	Maximum	Minimum	Most Likely	Maximum
Oil Gravity	30	35	40	30	35	40	30	35	40
Gas-Oil Ratio	500	1,000	1,500	500	1,000	1,500	500	1,000	1,500
Gas Gravity	0.65	0.70	0.75	0.65	0.70	0.75	0.65	0.70	0.75
Pgr, psi	0.44	0.45	0.48	0.44	0.45	0.48	0.44	0.45	0.48
Depth, m	4,000	4,250	4,550	4,625	4,850	5,150	2,360	2,460	2,560
Porosity	15	22	30	15	22	30	15	22	30
Water Sat.	20	30	40	20	30	40	20	30	40
Drainage area, km <sup>2</sup>	32	51	77	37	50	73	6	11	15
Gross Thickness, m	100	140	180	100	125	175	30	40	50
Net/Gross, fraction	0.25	0.45	0.65	0.25	0.45	0.65	0.25	0.45	0.65
% Recovery	19.00	28.00	35.00	18.00	28.00	35.00	19.00	28.00	35.00

# Example Results



# Example Results

Lead	Prospective Oil Equivalent Resource, MMBOE <sub>g</sub>		
	Low Estimate	Best Estimate	High Estimate
Joe (Tert)	62.7	148.3	280.7
Jimmy (Tert)	12.6	35.5	81.0
Amatuk (U Cret)	100.6	228.3	428.2
KC (U Cret)	20.3	41.1	73.3
KC-A (U Cret)	35.5	63.5	109.5
Hammerhead (Tert)	6.2	11.0	19.0
MJ-3 (U Cret)	124.1	230.1	402.3
KB (Tert)	167.6	349.5	689.1
KG (U Cret)	339.7	633.5	1,058.3
Jethro Ext (Tert)	15.6	46.1	91.7
Rappu (U Cret)	247.1	535.6	1,002.9
DJ (U Cret)	85.6	150.0	244.9
Kumaka (U Cret)	335.0	667.5	1,236.7
Jethro (Tert)	114.9	214.5	372.0
Iatuk-D (U Cret)	348.2	627.2	1,125.4
<b>Total</b>	<b>2,015.8</b>	<b>3,981.9</b>	<b>7,215.0</b>

# Mongolia Example

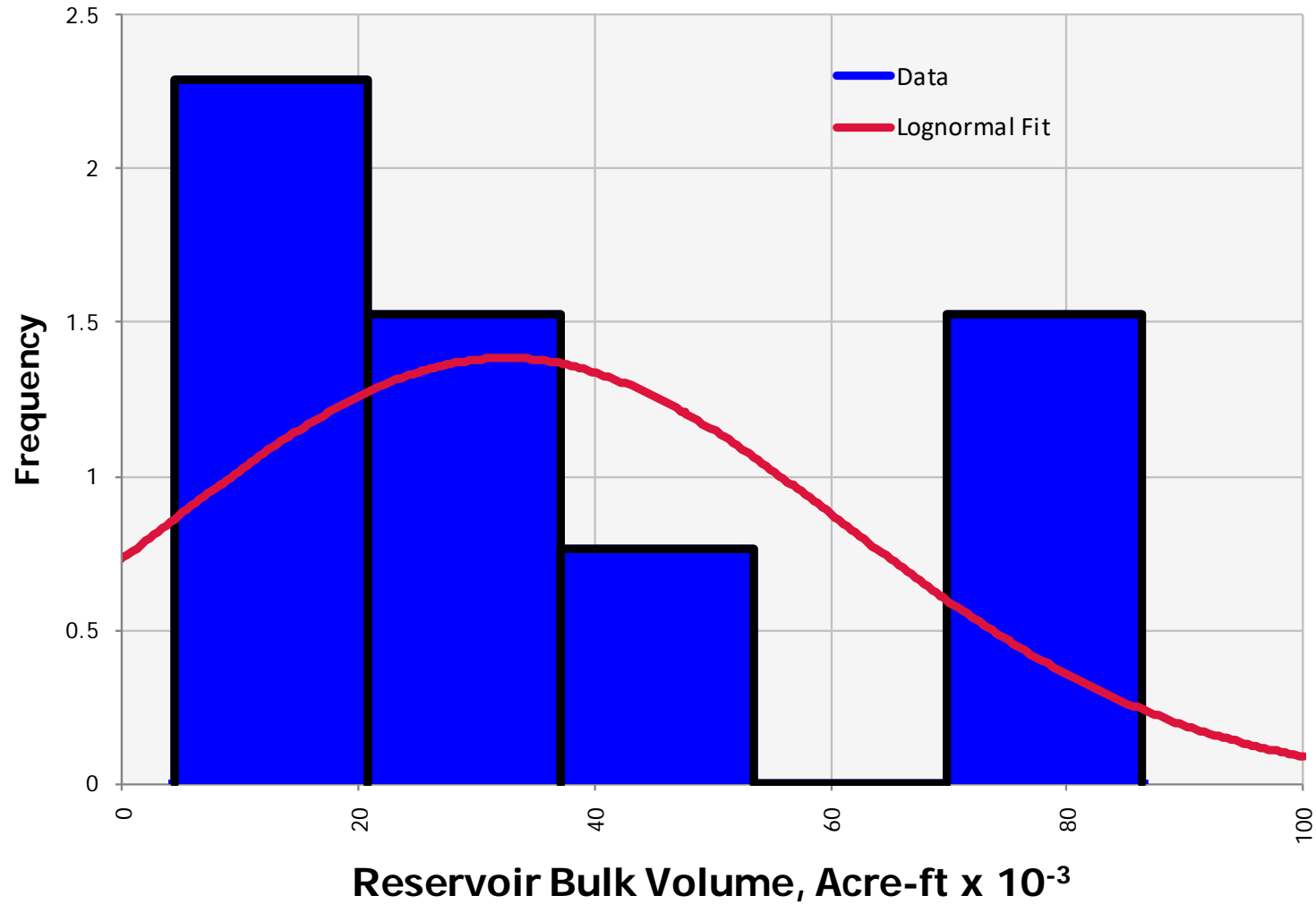
- Conventional exploration targets
- Data limited to extensive gravity surveys and sparse 2D seismic coverage
- Methodology used is a statistical approach based on the analogy of the currently producing fields in nearby blocks

# Input Data

<b>Parameter</b>	<b>Units</b>	<b>Minimum</b>	<b>Most Likely</b>	<b>Maximum</b>
Oil Gravity	°API	22	27.9	33.5
Solution Gas-Oil Ratio	cuft/bbl	97	124	169
Gas Gravity	Relative to air	0.60	0.65	0.70
Temperature gradient	°F/ft	0.0164	0.0169	0.0174
Pressure gradient	psi/ft	0.43	0.44	0.45
Depth	ft	1,394	4,265	8,203
Porosity	%	11	13	15
Water Sat.	%	30	35	40
% Recovery		12%	17%	30%
# Prospects Block XIII		5	12	18
# Prospects Block XIV		4	11	18

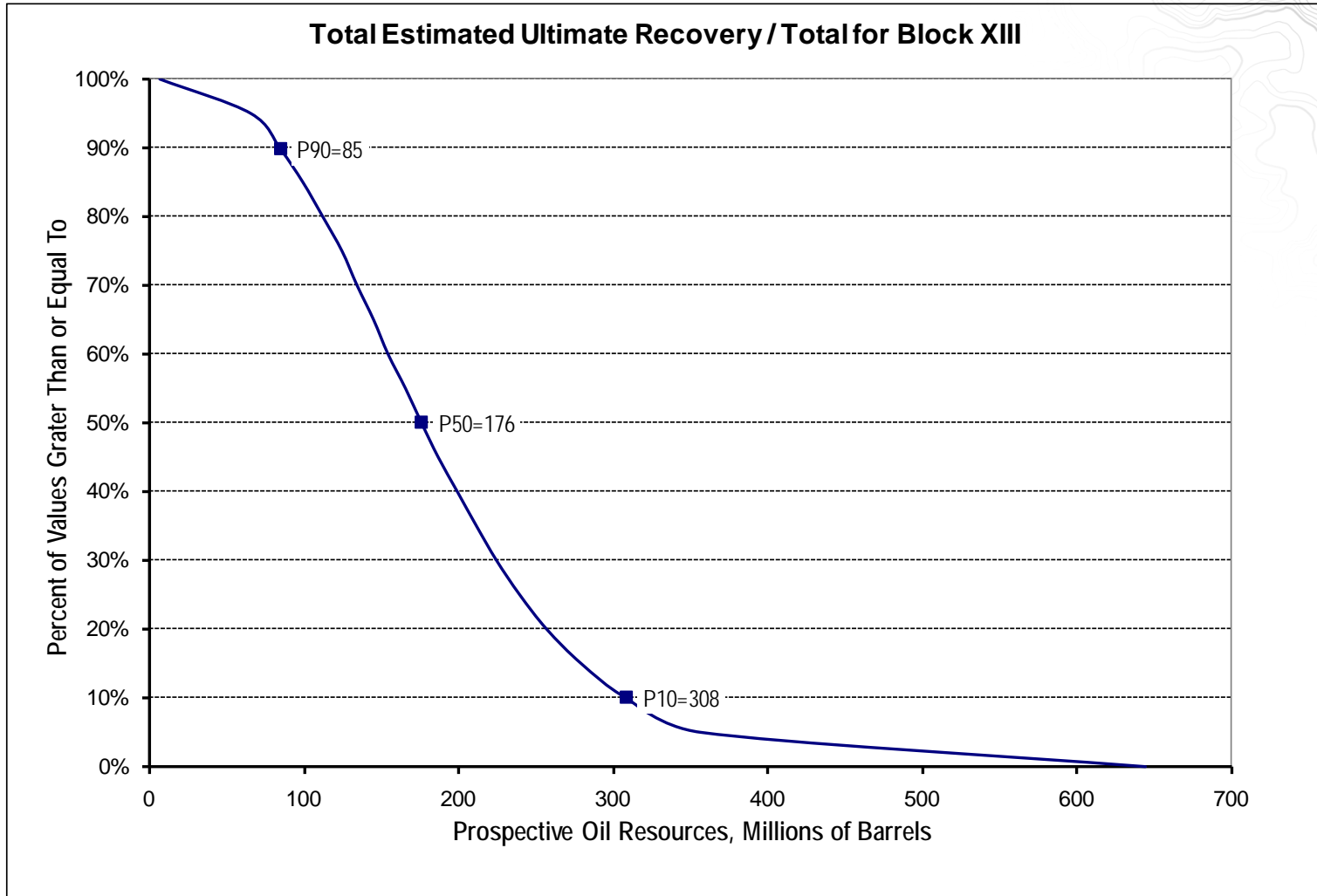
# Fit Comparison for Distribution of Reservoir Bulk Volume per Sand

Lognormal Distribution, truncated at zero





# Example Output



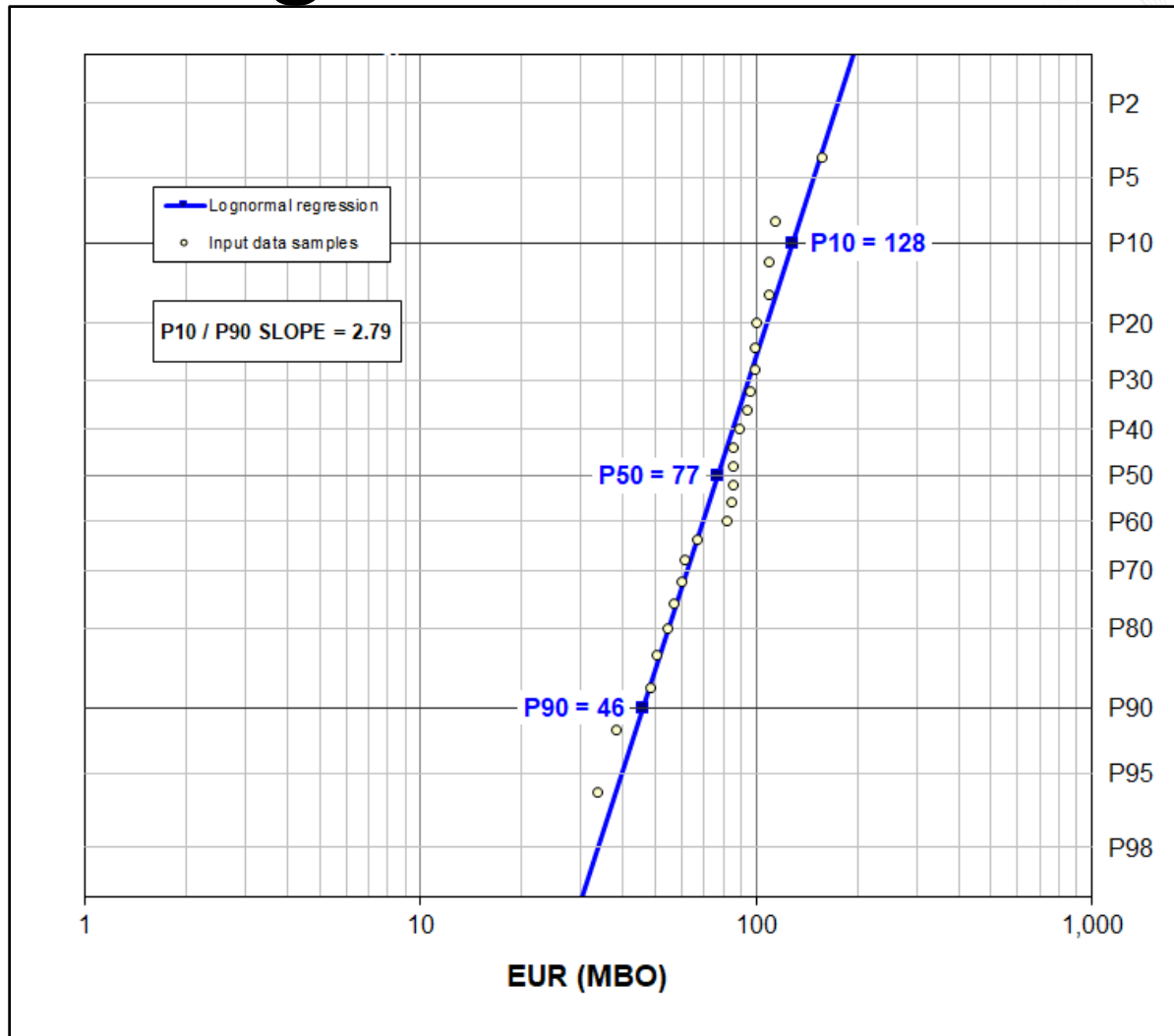
# Summary of Estimates

	<b>Prospective Oil Resources, Millions of Barrels</b>		
<b>Block</b>	<b>Low Estimate</b>	<b>Best Estimate</b>	<b>High Estimate</b>
XIII	85	176	308
XIV	78	165	293
<b>Sum of Prospects</b>	<b>163</b>	<b>341</b>	<b>602</b>

# Austin Chalk Example

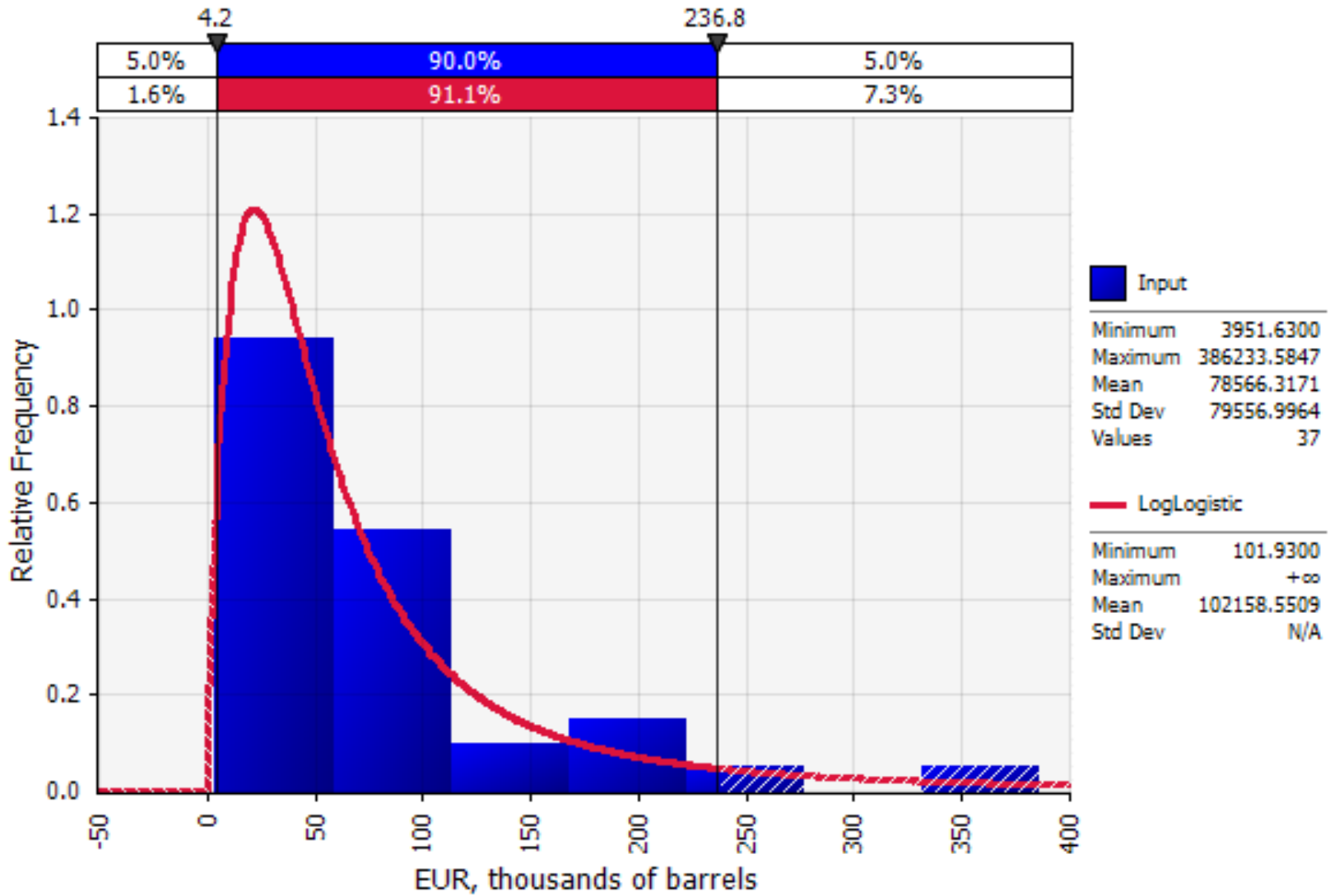
- Resource Play
- Known reservoir – penetrated and produced from numerous vertical wells
- No horizontal wells nearby
- Designated Contingent Resources
  - Estimated based on statistics of nearest horizontal wells' EURs
  - Input distribution for number of wells to be drilled
  - Multiple samplings of EUR distribution for each iteration

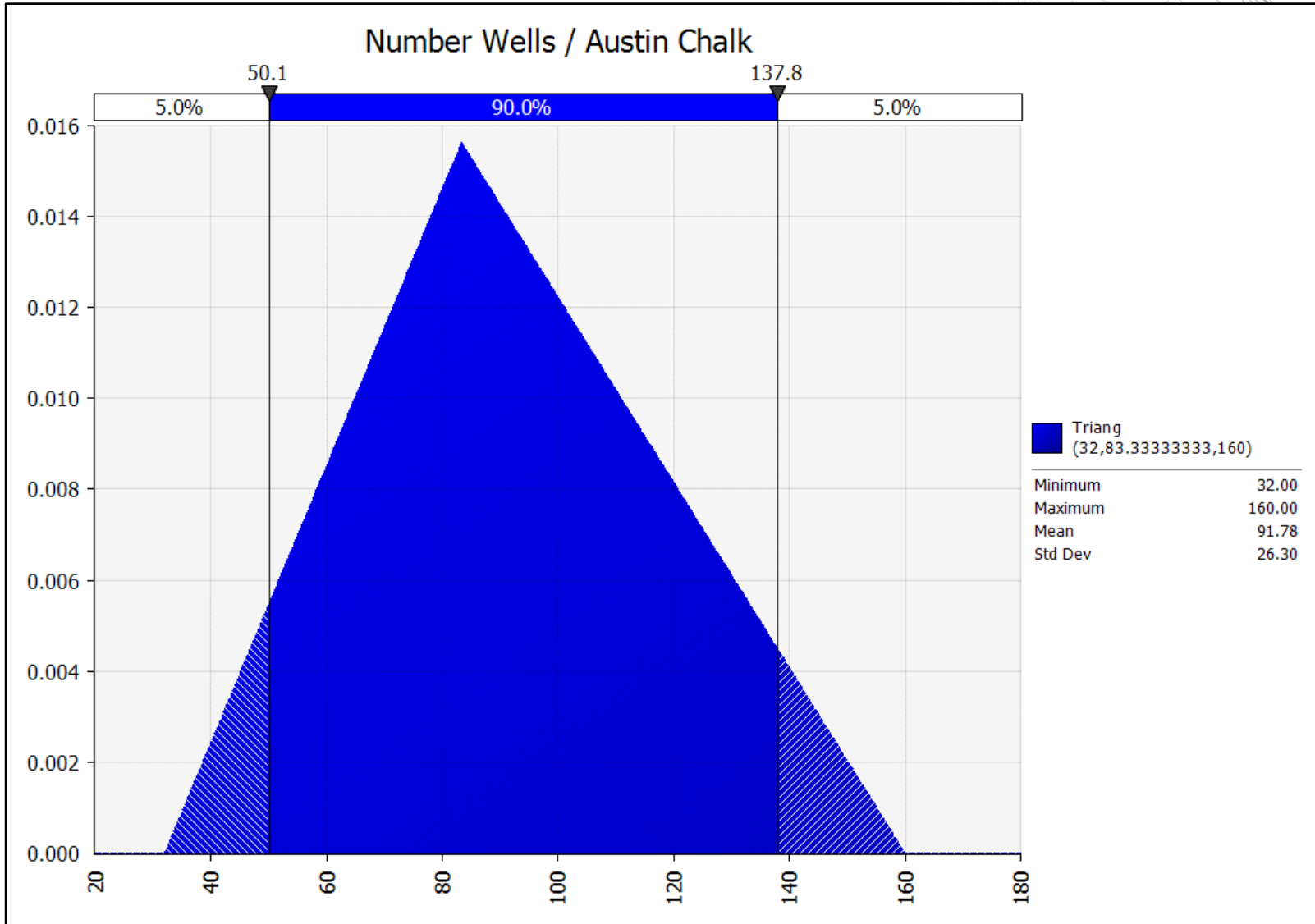
# Log Cum Probit Plot

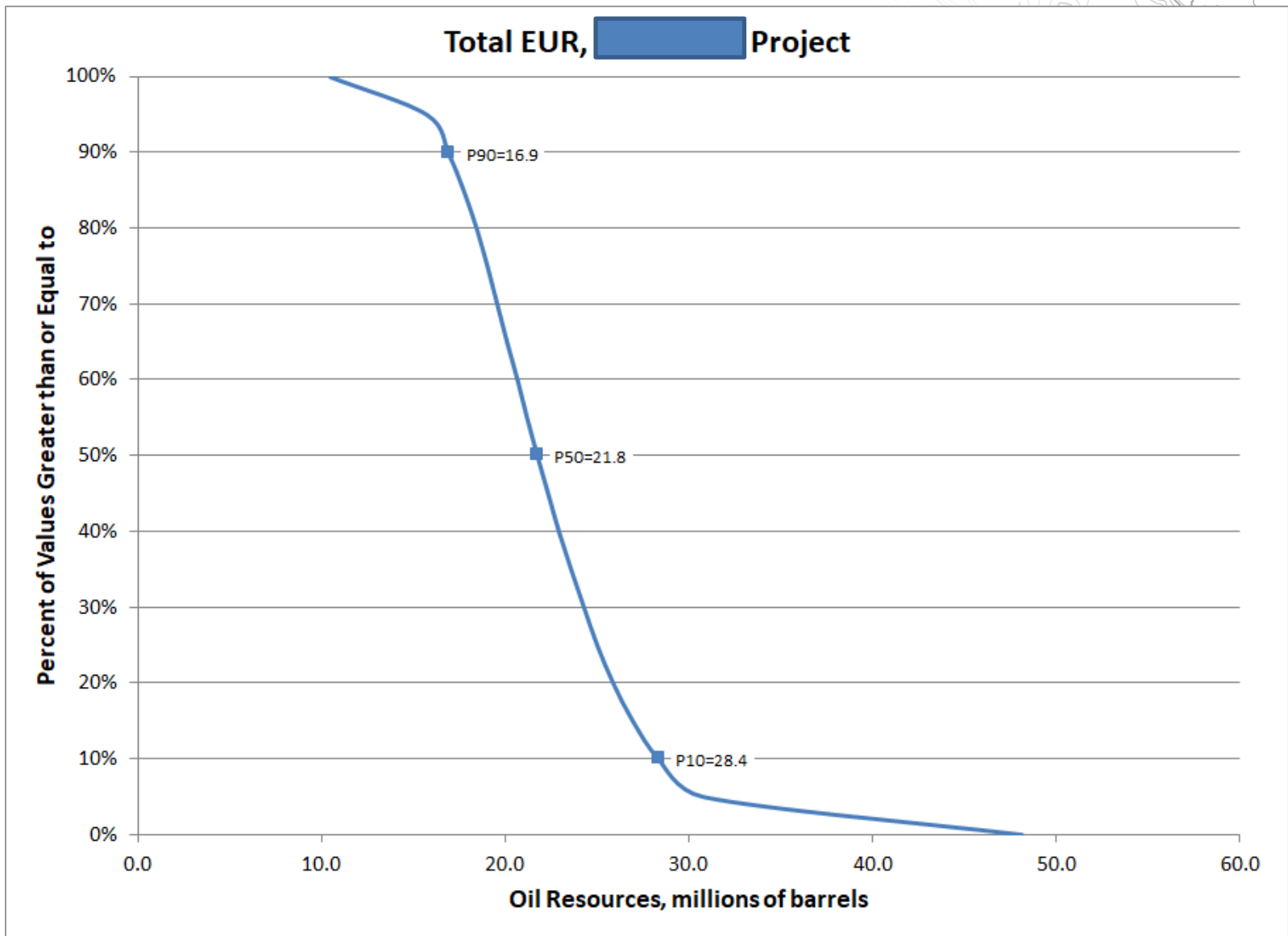


# Histogram and Distribution Fit to Austin Chalk EURs

RiskLogLogistic(101.93,50587,1,6487)







# Bangladesh Example

- Modeled identified exploratory prospects individually
- Modeled unmapped conventional resources based on a USGS study
  - Divided the country into six regions and did a probabilistic assessment of the number of fields within each region and the resource size for each field
  - Our model used the same regions and a simplified version of the USGS probabilistic modeling of success rates, discoveries, and field sizes.



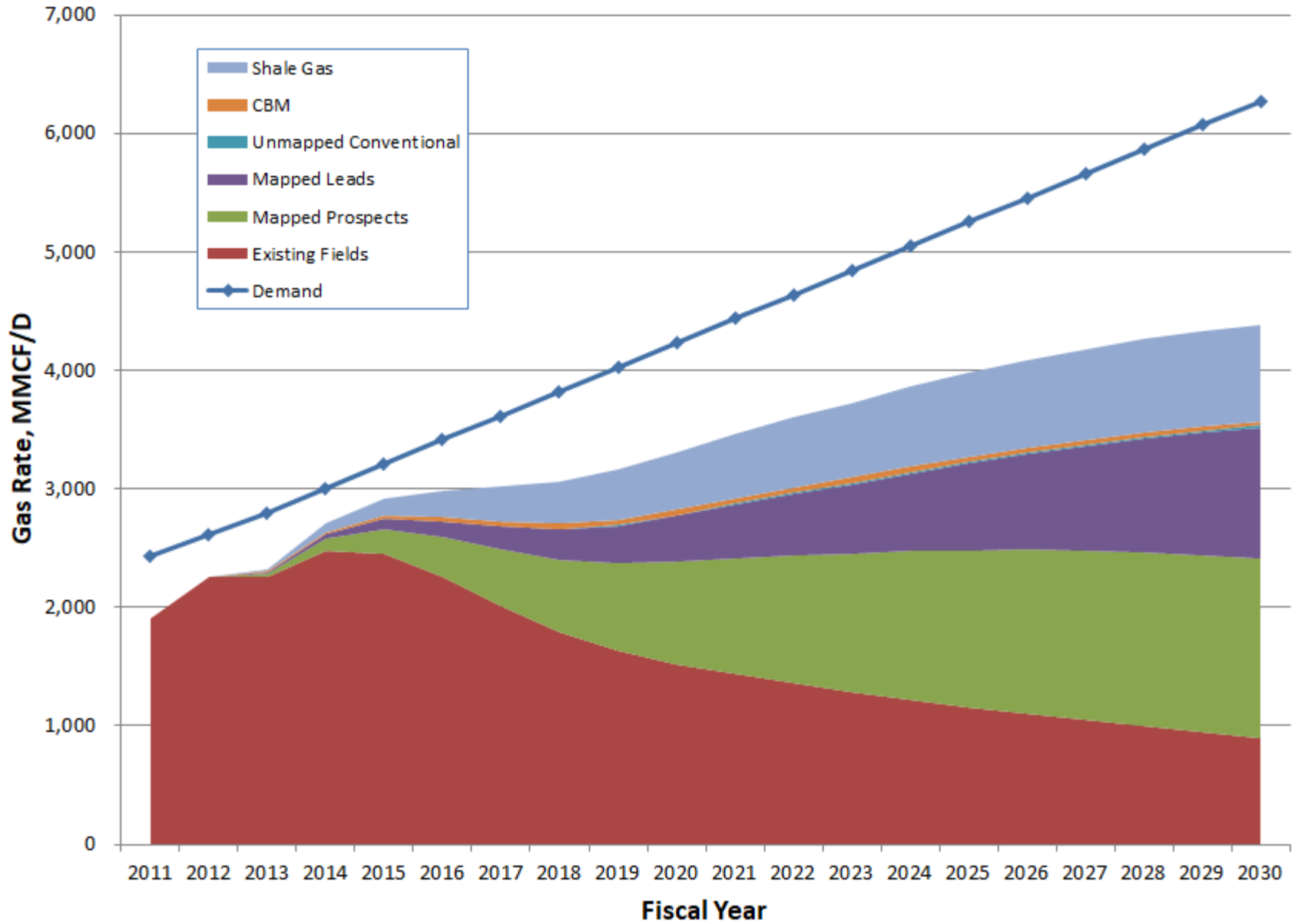
# Bangladesh Example

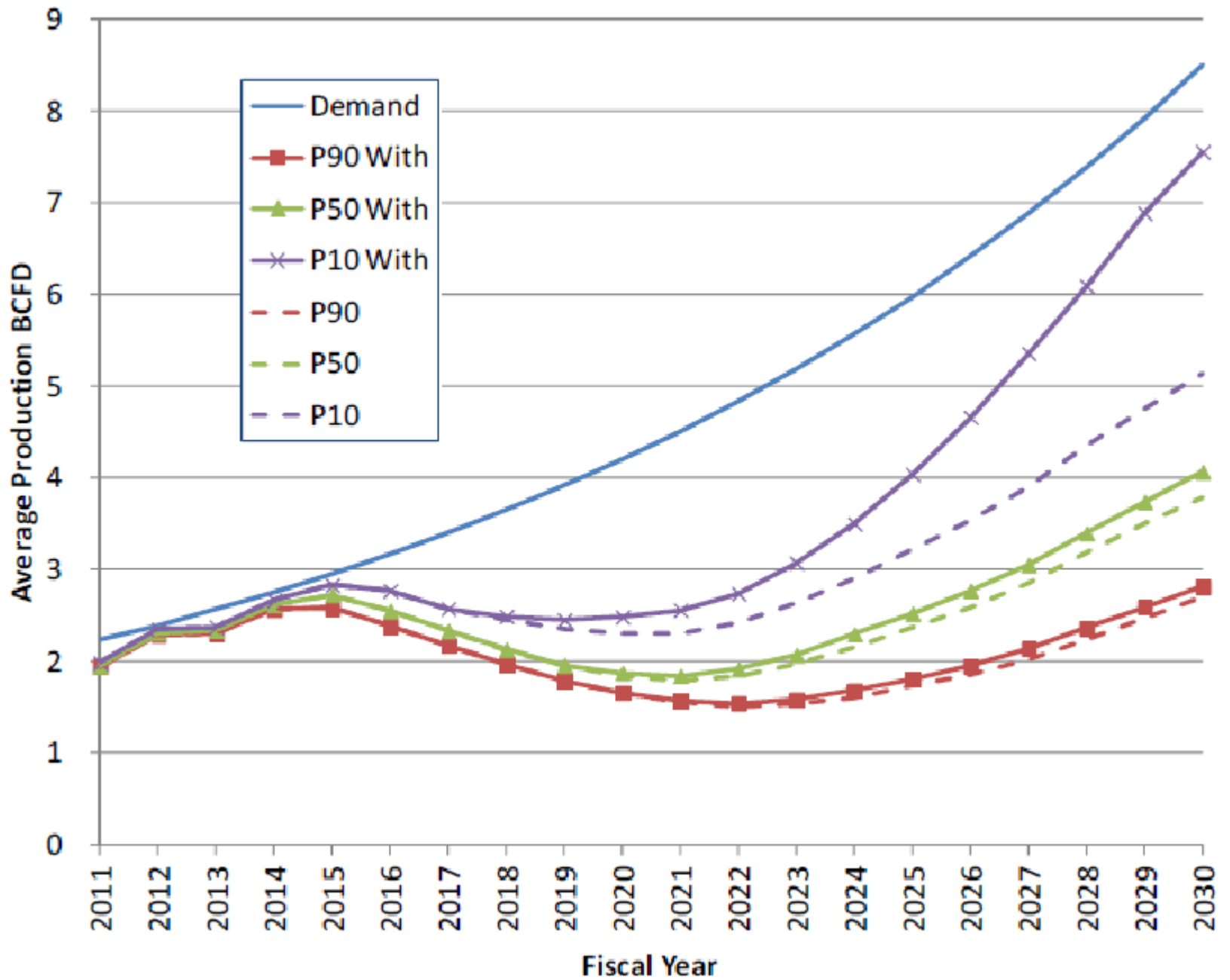
- Unconventionals
  - CBM
    - Estimated for each known coal deposit in Bangladesh
    - Resource estimates based on expected ranges of area, net coal thickness, density, gas content, and recovery factor
  - Shale gas
    - Four potential shale plays identified
    - Resource estimates based on expected ranges of area, thickness, and recoverable gas per acre-ft

# Bangladesh Example

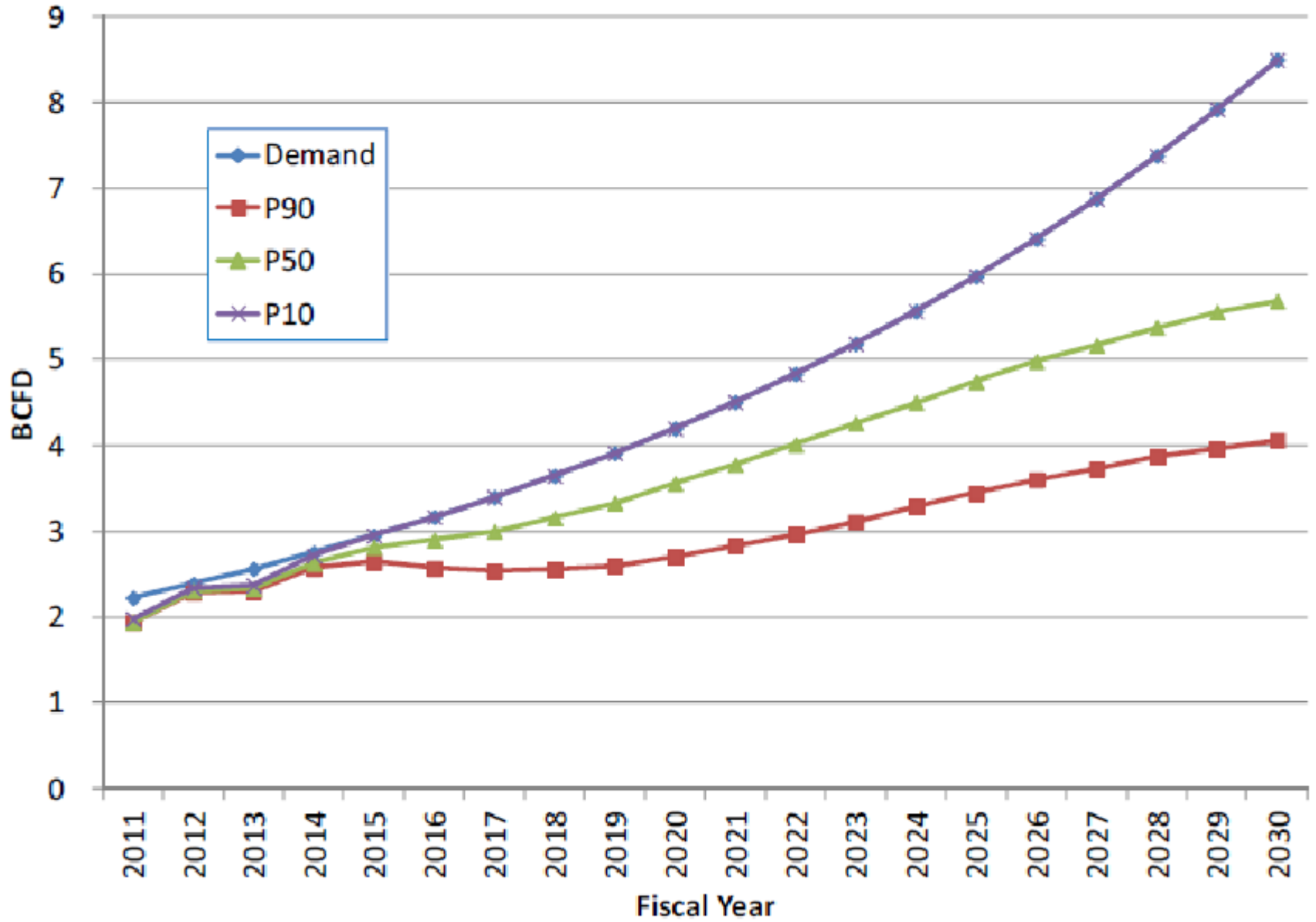
- Future gas supply and demand scenarios were also modeled
  - Three deterministic demand scenarios
  - Reserves forecast probabilistically
  - Each type of resource (prospects, unmapped conventional, CBM, and shale gas) modeled separately
  - POS considered, and assumptions about exploration schedule modeled

# Mean Forecast Production, Mid-Demand Case, MMCF/D





# Annual Average Gas Rates - Accelerated Exploration

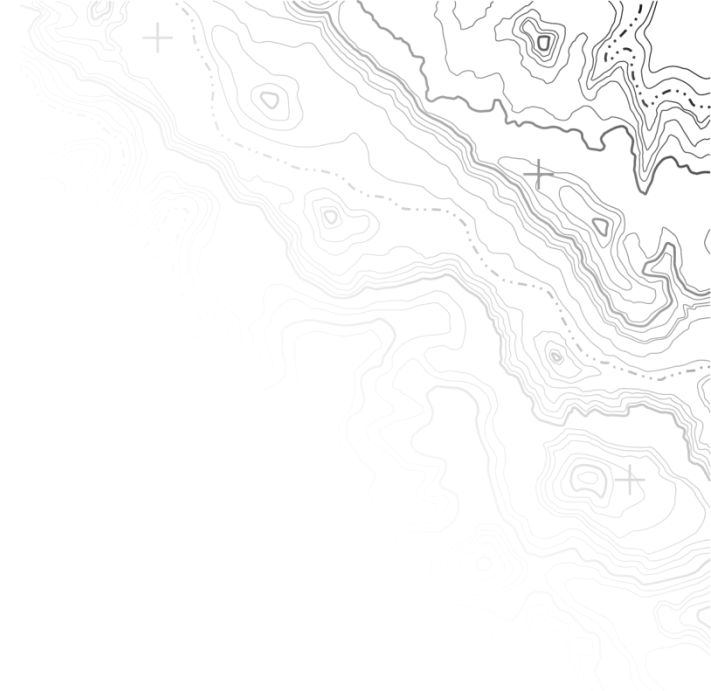


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Thanks to Gustavson Associates, and our clients.

**QUESTIONS?**